

Class – 10 Science

Notes

Chapter-12 Electricity

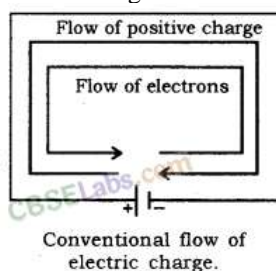
Electricity: Electric current, electric circuit, voltage or electric potential, resistance and (Ohm's law).

Electric Current: The flow of electric charge is known as Electric Current, Electric current is carried by moving electrons through a conductor.

By convention, electric current flows in the opposite direction to the movement of electrons.

Electric Circuit: Electric circuit is a continuous and closed path of electric current.

Expression of Electric Current: Electric current is denoted by the letter 'I'. Electric current is expressed by the rate of flow of electric charges. Rate of flow means, the amount of charge flowing through a particular area in unit time.



If a net electric charge (Q) flows through a cross-section of a conductor in time t, then,

$$\text{Electric current (I)} = \frac{\text{Net charge (Q)}}{\text{Time (t)}} \quad \text{or,} \quad \boxed{I = \frac{Q}{t}}$$

Where I is electric current, Q is a net charge and t is a time in second.

S.I. Unit of Electric Charge and Current: S.I. unit of electric charge is coulomb (C).

One coulomb is nearly equal to 6×10^{18} electrons. S.I. unit of electric current is ampere (A). Ampere is the flow of electric charge through a surface at the rate of one coulomb per second. This means, if 1 coulomb of electric charge flows through a cross section for 1 second, it would be equal to 1 ampere.

Therefore, $1 \text{ A} = 1 \text{ C/1 s}$

Small Quantity of Electric Current: Small quantity of electric current is expressed in milliampere and microampere. Milliampere is written as mA and microampere as μA .

$1 \text{ mA (milliampere)} = 10^{-3} \text{ A}$

$1 \text{ } \mu\text{A (microampere)} = 10^{-6} \text{ A}$

Ammeter: An apparatus to measure electric current in a circuit.,

Charge: Like mass, the charge is the fundamental property of matter. There are two types of charge

- (i) Positive charge.
- (ii) Negative charge.

Positive and Negative Charge: The charge acquired by a glass rod when rubbed with silk is called a positive charge and the charge acquired by an ebonite rod when rubbed with wool is called negative charge.

Properties of Electric Charge:

- (i) Unlike charges attract each other and like charges repel each other.
- (ii) The force between two charges varies directly as the product of two charges and inversely as the square of the distance (r) between both charges (q_1 and q_2).

$$F \propto \frac{q_1 \times q_2}{r_2^2} \quad F = K \frac{q_1 \times q_2}{r_2^2}$$

$K = \text{constant}$

S.I. unit of charge is coulomb (C).

1 coulomb = 1 ampere \times 1 second.

1C = 1A \times 1s

Thus, the quantity of charge which flows through a circuit when one ampere of current flows through it in one second is known as a 1-coulomb charge.

Electric Potential and Potential Difference

Electric Potential: The amount of electric potential energy at a point is called electric potential.

Potential Difference: The difference in the amount of electric potential energy between two points in an electric circuit is called electric potential difference.

Electric potential difference is known as voltage, which is equal to the amount of work done to move the unit charge between two points against static electric field.

Therefore, Voltage = $\frac{\text{Workdone}}{\text{Charge}}$

Voltage or electric potential difference is denoted by 'V'. Therefore, $V = \frac{W}{Q}$

Where, W = Work done and Q = Charge

S.I. Unit of Electric Potential Difference (Voltage)

S.I. unit of electric potential difference is volt and denoted by 'V' This is named in honour of Italian Physicist Alessandro Volta.

Since joule is the unit of work and Coulomb is the unit of charge, 1 volt of electric potential difference is equal to the 1 joule of work to be done to move a charge of 1 coulomb from one point to another in an electric circuit. Therefore

1V = 1Joule/1Coulomb = 1J/1C

1V = 1JC⁻¹

Voltmeter: An apparatus to measure the potential difference or electric potential difference between two points in an electric circuit.

Galvanometer: It is a device to detect current in an electric circuit.

Ohm's Law: Ohm's Law states that the potential difference between two points is directly proportional to the electric current, at a constant temperature.

This means potential difference V varies as electric current.

$V \propto I$

$V = RI$

$I = \frac{V}{R}$

$R = \frac{V}{I}$

Where, R is constant for the given conductor at a given temperature and is called resistance.

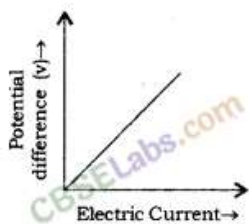
Resistance: Resistance is the property of conductor which resists the flow of electric current through it.

S.I. unit of resistance is ohm. Ohm is denoted by Greek letter 'Q'

1 Ohm: 1 ohm (Q) of resistance (R) is equal to the flow 1A of current through a conductor between two points having a potential difference equal to 1V.

This means; $1\Omega = 1V/1A$

From the expression of Ohm's Law, it is obvious that electric current through a resistor is inversely proportional to resistance. This means electric current will decrease with an increase in resistance and vice versa. The graph of V (potential difference) versus I (electric current) is always a straight line.



Graph of Potential Difference (V) Vs Electric Current (I)

Voltage, i.e. Potential difference (V) = ?

We know, from Ohm's Law that,

$$R = V/I$$

$$15 \Omega = V/15A$$

$$V = 225V$$

Resistance: Resistance is a property of conductor due to which it resists the flow of electric current through it. A component that is used to resist the flow of electric current in a circuit is called a resistor.

In practical application, resistors are used to increase or decrease the electric current.

Variable Resistance: The component of an electric circuit which is used to regulate the current, without changing the voltage from the source, is called variable resistance.

Rheostat: This is a device which is used in a circuit to provide variable resistance.

Cause of Resistance in a Conductor: Flow of electrons in a conductor is electric current. The positive particles of conductor create hindrance to flow of electrons, because of attraction between them, this hindrance is the cause of resistance in the flow of electricity.

Factors on Which Resistance of a Conductor Depends: Resistance in a conductor depends on nature, length and area of cross section of the conductor.

(i) Nature of Material: Some materials create least hindrance and hence, are called good conductors. Silver is the best conductor of electricity. While some other materials create more hindrance in the flow of electric current, i.e. flow of electrons through them. Such materials are called bad conductors. Bad conductor are also known as insulators. Hard plastic is the one of the best insulators of electricity.

(ii) Length of Conductor: Resistance (R) is directly proportional to the length of the conductor. This means, resistance increases with increase in length of the conductor. This is the cause that long electric wires create more resistance to the electric current. Thus, Resistance (R) \propto length of conductor (l)
or, $R \propto l$... (i)

(iii) Area of Cross Section: Resistance R is inversely proportional to the area of cross section (A) of the conductor. This means R will decrease with an increase in the area of conductor and vice versa. More area of conductor facilitates the flow of electric current through more area and thus, decreases the resistance. This is the cause that thick copper wire creates less resistance to the electric current.

Thus, resistance (R) \propto 1/Area of cross section of conductor (A)

or, $R \propto 1/A$... (ii)

From equations (i) and (ii)

$$R \propto l/A$$

$$R = \rho l/A$$

Where, ρ (rho) is the proportionality constant. It is called the electrical resistivity of the material of conductor.

From equation (iii) $RA = \rho l \Rightarrow \rho = RA/l$... (iv)

The S.I. of Resistivity: Since, the S.I. unit of R is Q, S.I. unit of area is m^2 and S.I. unit of length is m. Hence, unit of resistivity (ρ) = $\Omega \times m^2/m = \Omega m$

Thus, S.I. unit of resistivity (ρ) is Ωm .

Resistivity: It is defined as the resistance offered by a cube of a material of side 1m when current flows perpendicular to its opposite faces. It's S.I. unit is ohm-meter (Ωm).

$$\text{Resistivity, } \rho = RA/l$$

Resistivity is also known as specific resistance.

Resistivity depends on the nature of the material of the conductor.

Materials having a resistivity in the range of $10^{-8} \Omega m$ to $10^{-6} \Omega m$ are considered as very good conductors. Silver has resistivity equal to $1.60 \times 10^{-8} \Omega m$ and copper has resistivity equal to $1.62 \times 10^{-8} \Omega m$.

Rubber and glass are very good insulators. They have a resistivity in the order of $10^{12} \Omega m$ to $10^{-8} \Omega m$.

The resistivity of materials varies with temperature.

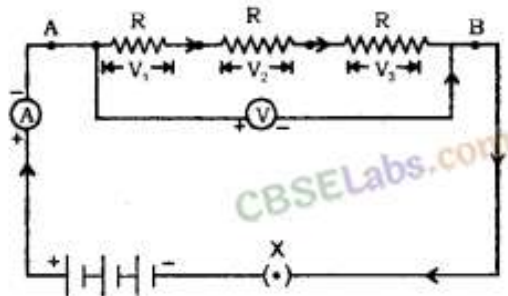
Combination of resistors (Series and Parallel combination), the heating effect of electric current and electric power.

Combination of Resistors

(i) Series combination

(ii) Parallel combination.

1. Resistors in Series: When resistors are joined from end to end, it is called in series. In this case, the total resistance of the system is equal to the sum of the resistance of all the resistors in the system.



Let, three resistors R_1 , R_2 , and R_3 get connected in series.

Potential difference across A and B = V

Potential difference across R_1 , R_2 and $R_3 = V_1, V_2$ and V_3

Current flowing through the combination = I

We, know that

$$V = V_1 + V_2 + V_3 \dots (i)$$

According to Ohm's Law :

$$V_1 = IR_1, V_2 = IR_2 \text{ and } V_3 = IR_3 \dots (ii)$$

Let, total resistance = R_s

$$\text{Then, } V = IR_s \dots (iii)$$

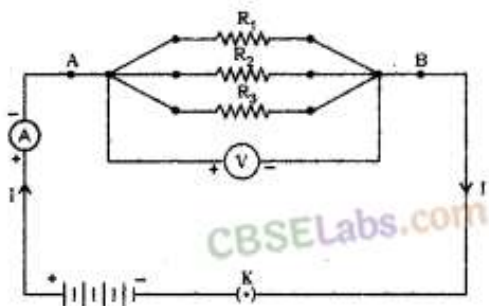
From equations (i) and (ii) and (iii)

$$IR_s = IR_1 + IR_2 + IR_3$$

$$R_s = R_1 + R_2 + R_3$$

When the resistors are connected in series, the current flowing through each resistor is the same and is equal to the total current.

2. Resistors in Parallel: When resistors are joined in parallel, the reciprocal of the total resistance of the system is equal to the sum of reciprocal of the resistance of resistors.



Let three resistors R_1 , R_2 and R_3 connected in parallel.

Potential difference across point A and B = V

Total current flowing between point A and B = I

Currents flowing through resistors R_1 , R_2 and $R_3 = I_1, I_2$ and I_3 respectively.

We, know that,

$$I = I_1 + I_2 + I_3 \dots (i)$$

Since, the potential difference across R_1 , R_2 , and R_3 is the same = V

According to Ohm's Law,

$$I_1 = \frac{V}{R_1}, I_2 = \frac{V}{R_2} \text{ and } I_3 = \frac{V}{R_3} \quad \dots\dots(ii)$$

Let, Total Resistance = R_p

$$\text{Thus, } I = \frac{V}{R_p} \quad \dots(iii)$$

From equations (i), (ii) and (iii)

$$\frac{V}{R_p} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3} \quad \Rightarrow \quad \frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \quad \dots(iv)$$

In parallel combination, the potential difference across each resistor is the same and is equal to the total potential difference.

The total current through the circuit can be calculated by adding the electric current through individual resistors.

$$I_{\text{total}} = 6A + 48A + 30A + 12A + 24A = 120A$$

Heating Effect of Electric Current: When electric current is supplied to a purely resistive conductor, the energy of electric current is dissipated entirely in the form of heat and as a result, resistor gets heated. The heating of resistor because of dissipation of electrical energy is commonly known as Heating Effect of Electric Current. Some examples are as follows : When electric energy is supplied to an electric bulb, the filament gets heated because of which, it gives light. The heating of electric bulb happens because of heating effect of electric current.

Cause of Heating Effect of Electric Current: Electric current generates heat to overcome the resistance offered by the conductor through which it passes. Higher the resistance, the electric current will generate higher amount of heat. Thus, generation of heat by electric current while passing through a conductor is an inevitable consequence. This heating effect is used in many appliances, such as electric iron, electric heater, electric geyser, etc.

Joule's Law Of Heating: Let, an electric current, I is flowing through a resistor having resistance = R .

The potential difference through the resistor is = V .

The charge, Q flows through the circuit for the time, t

Thus, work done in moving of charge (Q) of potential difference (V),

$$W = V \times Q$$

Since this charge, Q flows through the circuit for time t

Therefore, power input (P) to the circuit can be given by the following equation :

$$P = \frac{W}{t}$$

$$P = V \times \frac{Q}{t} \quad \dots(i)$$

We know, electric current, $I = \frac{Q}{t}$

Substituting $\frac{Q}{t} = I$ in equation (i), we get,

$$P = VI \quad \dots(ii)$$

i.e., $P = VI$

Since, the electric energy is supplied for time t , thus, after multiplying both sides of equation (ii) by time t , we get,

$$P \times t = VI \times t = VI t \quad \dots(iii)$$

i.e., $P = VI t$

Thus, for steady current I , the heat produced (H) in time t is equal to $VI t$

$$H = VI t \text{ i.e., } H = VI t$$

We know, according to Ohm's Law,

$$V = IR$$

By substituting this value of V in equation (iii), we get,

$$H = IR \times I t$$

$$H = I^2 R t \quad \dots(iv)$$

The expression (iv) is known as Joule's Law of Heating, which states that heat produced in a resistor is directly proportional to the square of current given to the resistor, directly proportional to the resistance for a given current and directly proportional to the time for which the current is flowing through the resistor.

Electric Bulb: In an electric bulb, the filament of bulb gives light because of the heating effect of electricity. The filament of bulb is generally, made of tungsten metal, having melting point equal to 3380°C .

Electric Iron: The element of electric iron is made of alloys having high melting point. Electric heater and geyser work on the same mechanism.

Electric Fuse: Electric fuse is used to protect the electric appliances from high voltage if any. Electric fuse is made of metal or alloy of metals, such as aluminum, copper, iron, lead, etc. In the case of flow of higher voltage than specified, fuse wire melts and protect the electric appliances.

Fuse of 1A, 2A, 3A, 5A, 10A, etc., used for domestic purpose.

Suppose, if an electric heater consumes 1000W at 220 V.

Then electric current in circuit

$$I = PV$$

$$I = 1000W/220V = 4.5 \text{ A}$$

Thus, in this case of 5A should be used to protect the electric heater in the flow of higher voltage.

Electric Power

S.I. unit of electric power is watt (W).

$$1W = 1 \text{ volt} \times 1 \text{ ampere} = 1V \times 1A$$

1 kilowatt or 1kW = 1000 W

Consumption of electricity (electric energy) is generally measured in kilowatt.

Unit of electric energy is kilowatt-hour (kWh).

$$1 \text{ kWh} = 1000 \text{ watt} \times 1 \text{ hour} = 1 \text{ unit} = 1000 \text{ W} \times 3600 \text{ s}$$

$$1 \text{ kWh} = 3.6 \times 10^6 \text{ watt second} = 3.6 \times 10^6 \text{ J}$$

Conductor: The material which can allow the flow of electrons through itself is called the conductor. It has a large number of free electrons. It offers low opposition in the flow of current.

Insulator: The material which does not allow the flow of electrons through itself is called insulator. It has less or no free electrons. It offers high opposition in the flow of current.

Electric Current: The amount of flow charge through any cross-sectional area of a conductor in unity time is called Electric Current. It is represented by 'I'

$$I = QT$$

Unit of Electric Current: It is CS^{-1} (coulomb per second) or Ampere (A). Electric Current is a scalar quantity. It is measured by an ammeter.

Direction: The direction of conventional current (or practical current) is opposite to the flow of electrons.

Electric potential: Electric Potential at any point in the electric field is defined as the amount of work done to bring the unit positive charge from infinity (from outside the electric field) to that point.

$V = W/Q$, S.I. unit of Electric Potential is JC^{-1} or volt (V). It is a scalar quantity. The +ve charge flows from higher to lower potential.

The -ve charge flows from lower to a higher potential. The difference of electric potential between any two points in the electric field is called Electric Potential difference. It is known as a voltage which is equal to the work done per unit charge between two points against the static electric field.

$$V_{AB} = V_A - V_B = W_{AB}/Q$$

Electric Potential difference is measured by a voltmeter.

Ohm's Law: According to this law "Under the constant physical condition the potential difference across the conductor is directly proportional to the current flowing through the conductor."

$$V \propto I$$

$$V = IR \dots [\text{Where } R \text{ is proportionality constant called resistance of conductor}]$$

$$\Rightarrow I = VR$$

R depends upon nature, geometry and physical condition of the conductor.

The heat generated by electric current: The potential difference between two points in an electrical field is equal to the work done in moving a unit charge from one point to another.

Then, work is done, $W = VQ$ and $Q = I \times t$

$$W = V \times I \times t$$

From Ohm's Law, we know that

$$V = IR$$

$$W = IR \times I \times t = I^2.Rt$$

Since heat produced by the electric current is equal to work done, W

$$H = W$$

$$\Rightarrow H \text{ (heat)} = I^2 R t \text{ Joule.}$$

Resistance: Ratio of the applied voltage to the current flowing in the conductor is called resistance of the conductor.

$$\Rightarrow R = V/I$$

S.I. Unit of resistance is VA^{-1} or ohm (Ω).

Resistance is the opposition offered by the conductor in the flow of current.

Practically it is

$R \propto L$ (L is the length of a conductor)

$R \propto 1/A$ (A is the area of a conductor)

So, $R \propto L/A$

$R = \rho L/A$... [Where ρ is proportionality constant called specific resistance of conductor

It only depend upon nature (material) and temperature of conductor.

Specific resistance or Resistivity = $\rho = RA / L$

It's S.I. Unit is Ωm

Combination of resistance:

- In this combination the current across every component is same but potential across every component is different.
- If resistance R_1 , R_2 and R_3 are connected in series with a battery of Potential V , then equivalence resistance of the combination

$$R = R_1 + R_2 + R_3$$

The parallel combination of resistance:

- In this combination the current across every component is different. But potential across every component is the same.
- If resistance R_1 , R_2 and R_3 are connected in parallel with a battery of Potential V , then equivalence resistance of combination

$$1/R = 1/R_1 + 1/R_2 + 1/R_3$$

Electric Energy is amount of work done to maintain the continuous flow of electric current in the circuit.

Its S.I. unit is joule (J).

Electric power (P): The electric work done per unit time is called electric power.

Electric Power = $\frac{\text{Electric work done}}{\text{Time taken}}$

$$\text{or } P = W/t$$

Electric power is also defined as the electric energy consumed per unit time.

$$P = E/t$$

S.I. unit of electric power is Watt. When one joule of energy is used for one second, electric power is equal to one watt.

Derivation of formula for electric power:

We know that electric work done, $W = V \times I \times t$ or $P = VIt$

$$P = VI$$

Electric power in watts = Volts \times ampere

Also $V = IR$... [According to Ohm's Law]

So $P = IR \times I$

$$P = I^2 R$$

We know that $I = V/R$

$$P = (V/R)^2 \times R = V^2/R \text{ Watt}$$

The maximum value of electric current that can pass through an electric appliance without damaging electric appliance is called current rating of electric appliance.

Important Questions of Electricity

Question 1. A current of 10 A flows through a conductor for two minutes.

(i) Calculate the amount of charge passed through any area of cross section of the conductor.

(ii) If the charge of an electron is 1.6×10^{-19} C, then calculate the total number of electrons flowing. (Board Term I, 2013)

Answer: Given that: $I = 10$ A, $t = 2$ min = 2×60 s = 120 s

(i) Amount of charge Q passed through any area of cross-section is given by $I = Qt$

or $Q = I \times t \therefore Q = (10 \times 120)$ A s = 1200 C

(ii) Since, $Q = ne$

where n is the total number of electrons flowing and e is the charge on one electron

$\therefore 1200 = n \times 1.6 \times 10^{-19}$

or $n = 1200 / 1.6 \times 10^{-19} = 7.5 \times 10^{21}$

Question 2. Define electric current. (1/5, Board Term 1,2017)

Answer: Electric current is the amount of charge flowing through a particular area in unit time.

Question 3. Define one ampere. (1/5, Board Term 1,2015)

Answer: One ampere is constituted by the flow of one coulomb of charge per second.

$1 \text{ A} = 1 \text{ C s}^{-1}$

Question 4. Name a device that you can use to maintain a potential difference between the ends of a conductor. Explain the process by which this device does so. (Board Term I, 2013)

Answer: A cell or a battery can be used to maintain a potential difference between the ends of a conductor. The chemical reaction within a cell generates the potential difference across the terminals of the cell, even when no current is drawn from it. When it is connected to a conductor, it produces electric current and, maintain the potential difference across the ends of the conductor.

Question 5. Draw the symbols of commonly used components in electric circuit diagrams for

(i) An electric cell

(ii) Open plug key

(iii) Wires crossing without connection

(iv) Variable resistor

(v) Battery

(vi) Electric bulb

(vii) Resistance (4/5, Board Term 1,2017)

Answer:

S. No.	Component	Symbol
(i)	An electric cell	
(ii)	Open plug key	
(iii)	Wires crossing without connection	
(iv)	Variable resistor	
(v)	Battery	
(vi)	Electric bulb	
(vii)	Resistance	

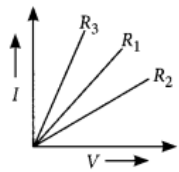
Question 6. A student plots V-I graphs for three samples of nichrome wire with resistances R_1 , R_2 and R_3 . Choose from the following the statements that holds true for this graph. (2020)

(a) $R_1 = R_2 = R_3$

(b) $R_1 > R_2 > R_3$

(c) $R_3 > R_2 > R_1$

(d) $R_2 > R_1 > R_3$



Answer: (d) : The inverse of the slope of I-V graph gives the resistance of the material. Here the slope of R_2 is highest. Thus, $R_2 > R_1 > R_3$

Question 7. State Ohms law. (AI 2019)

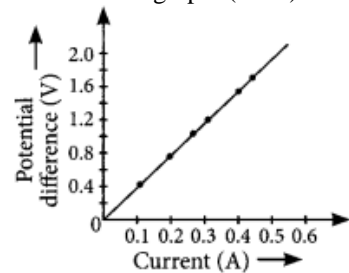
Answer: It states that the potential difference V , across the ends of a given metallic wire in an electric circuit is directly proportional to the current flowing through it, provided its temperature remains the same. Mathematically,

$$V \propto I$$

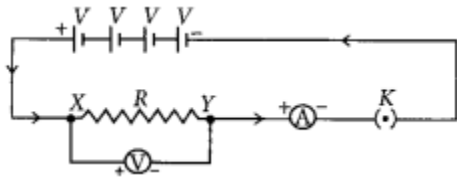
$$V = RI$$

where R is resistance of the conductor.

Question 8. A V-I graph for a nichrome wire is given below. What do you infer from this graph? Draw a labelled circuit diagram to obtain such a graph. (2020)

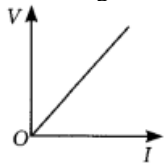


Answer: As graph is a straight line, so it is clear from the graph that $V \propto I$.



The shape of the graph obtained by plotting potential difference applied across conductor against the current flowing v . It will be a straight line.

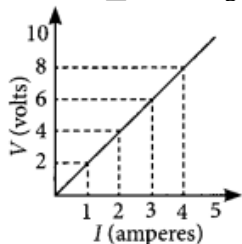
According to ohms law,



$$V = IR \text{ or } R = \frac{V}{I}$$

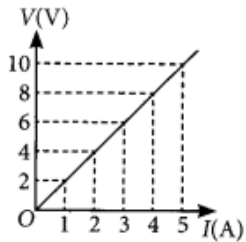
So, the slope of V - I graph at any point represents the resistance of the given conductor.

Question 9. Study the V-I graph for a resistor as shown in the figure and prepare a table showing the values of I (in amperes) corresponding to four different values V (in volts). Find the value of current for $V = 10$ volts. How can we determine the resistance of the resistor from this graph? (Board Term I, 2016)



Answer: Since, the graph is straight line so we can either extrapolate the data or simply mark the value from graph as shown in figure.

Current, I(A)	Voltage, V(V)
0	0
1	2
2	4
3	6
4	8



Hence, the value of current for $V = 10$ volts is 5 amperes (or 5 A).

From Ohm's law, $V = IR$,

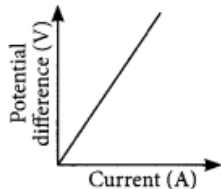
We can write, $R = V/I$

At any point on the graph, resistance is the ratio of values of V and I . Since, the given graph is straight line (ohmic conductor) so, the slope of graph will also give the resistance of the resistor

$$R = 10V/5A = 2\Omega$$

$$\text{Alternately, } R = (8-2)V/(4-1)A = 6V/3A = 2\Omega$$

Question 10. V-I graph for a conductor is as shown in the figure



- What do you infer from this graph?
- State the law expressed here. (Board Term I, 2014)

Answer:

- Refer to answer 8.
- Refer to answer 7.

Question 11. State Ohm's law. Draw a labelled circuit diagram to verify this law in the laboratory. If you draw a graph between the potential difference and current flowing through a metallic conductor, what kind of curve will you get? Explain how would you use this graph to determine the resistance of the conductor. (Board Term I, 2016)

Answer: Refer to answer 7 and 8.

Question 12. State and explain Ohm's law. Define resistance and give its SI unit. What is meant by 1 ohm resistance? Draw V-I graph for an ohmic conductor and list its two important features. (Board Term I, 2014)

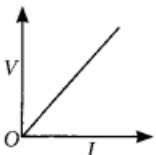
Answer: Ohm's law: Refer to answer 7.

Resistance : It is the property of a conductor to resist the flow of charges through it.

Its SI unit is ohm (Ω). If the potential difference across the two ends of a conductor is 1 V and the current through it is 1 A, then the resistance R , of the conductor is 1 ohm (1Ω). 1volt

$$1\text{ ohm} = 1\text{volt}/1\text{ampere}$$

V-I graph for an ohmic conductor can be drawn as given in figure.



Important feature of V-I graph are:

- (i) It is a straight line passing through origin.
- (ii) Slope of V-I graph gives the value of resistance of conductor slope = $R = V/I$

Question 13.

Assertion (A) : The metals and alloys are good conductors of electricity.

Reason (R) : Bronze is an alloy of copper and tin and it is not a good conductor of electricity.

- (a) Both (A) and (R) are true and (R) is the correct explanation of the assertion (A).
- (b) Both (A) and (R) are true, but (R) is not the correct explanation of the assertion (A).
- (c) (A) is true, but (R) is false.
- (d) (A) is false, but (R) is true. (2020)

Answer: (c) : Metals and alloys are good conductors of electricity. Bronze is an alloy of copper and tin which are metals and thus is a good conductor of electricity.

Question 14. A cylindrical conductor of length 'l' and uniform area of cross section 'A' has resistance 'R'. The area of cross section of another conductor of same material and same resistance but of length '2l' is (2020)

- (a) $2A$
- (b) $3A/2$
- (c) $2A$
- (d) $3A$

Answer: (c) : The resistance of a conductor of length l, and area of cross section, A is

$$R = \rho l/A$$

where ρ is the resistivity of the material.

Now for the conductor of length 2l, area of cross-section A' and resistivity ρ .

$$R' = \rho 2l/A' = \rho 2l/A$$

But given, $R = R' \Rightarrow \rho l/A = \rho 2l/A'$ or $A' = 2A$

Question 15. Assertion (A) : Alloys are commonly used in electrical heating devices like electric iron and heater.

Reason (R): Resistivity of an alloy is generally higher than that of its constituent metals but the alloys have low melting points than their constituent metals.

- (a) Both (A) and (R) are true and (R) is the correct explanation of the assertion (A).
- (b) Both (A) and (R) are true, but (R) is not the correct explanation of the assertion (A).
- (c) (A) is true, but (R) is false.
- (d) (A) is false, but (R) is true. (2020)

Answer: (a)

Question 16. How is the resistivity of alloys compared with those of pure metals from which they may have been formed? (Board Term I, 2017)

Answer: The resistivity of an alloy is generally higher than that of its constituent metals.

Question 17. (i) List three factors on which the resistance of a conductor depends.

(ii) Write the SI unit of resistivity. (Board Term 1, 2015)

Answer:

(i) Resistance of a conductor depends upon the following factors:

(1) Length of the conductor : (Greater the length (l) of the conductor more will be the resistance (R).

$$R \propto l$$

(2) Area of cross section of the conductor: (Greater the cross-sectional area of the conductor, less will be the resistance.

$$R \propto 1/A$$

(3) Nature of conductor.

(ii) SI unit of resistivity is $\Omega \text{ m}$.

Question 18. Calculate the resistance of a metal wire of length 2m and area of cross section $1.55 \times 10^{-6} \text{ m}^2$, if the resistivity of the metal be $2.8 \times 10^{-8} \Omega \text{ m}$. (Board Term I, 2013)

Answer: For the given metal wire,

length, $l = 2 \text{ m}$

area of cross-section, $A = 1.55 \times 10^{-6} \text{ m}^2$

resistivity of the metal, $\rho = 2.8 \times 10^{-8} \Omega \text{ m}$

Since, resistance, $R = \rho l/A$

So $R = (2.8 \times 10^{-8} \times 21.55 \times 10^{-6}) \Omega$

$= 5.61.55 \times 10^{-2} \Omega = 3.6 \times 10^{-2} \Omega$ or $R = 0.036 \Omega$

Question 19.

(a) List the factors on which the resistance of a conductor in the shape of a wire depends.

(b) Why are metals good conductors of electricity whereas glass is a bad conductor of electricity? Give reason.

(c) Why are alloys commonly used in electrical heating devices? Give reason. (2018)

Answer:

(a) Refer to answer 17 (i).

(b) Metal have very low resistivity and hence they are good conductors of electricity.

Whereas glass has very high resistivity so glass is a bad conductor of electricity.

(c) Alloys are commonly used in electrical heating devices due to the following reasons

(i) Alloys have higher resistivity than metals

(ii) Alloys do not get oxidised or burn readily.

Question 20. Calculate the resistivity of the material of a wire of length 1 m, radius 0.01 cm and resistance 20 ohms. (Board Term I, 2017)

Answer: We are given, the length of wire, $l = 1 \text{ m}$, radius of wire, $r = 0.01 \text{ cm} = 1 \times 10^{-4} \text{ m}$ and resistance, $R = 20 \Omega$ As we know, $R = \rho l/A$, where ρ is resistivity of the material of the wire.

$\therefore 20 \Omega = \rho l/\pi r^2 = \rho \times 1 / 3.14 \times (10^{-4})^2 \text{ m}^2$

$\therefore \rho = 6.28 \times 10^{-7} \Omega \text{ m}$

Question 21. A copper wire has diameter 0.5 mm and resistivity $1.6 \times 10^{-8} \Omega \text{ m}$. Calculate the length of this wire to make it resistance 100 Ω . How much does the resistance change if the diameter is doubled without changing its length? (Board Term I, 2015)

Answer: Given; resistivity of copper = $1.6 \times 10^{-8} \Omega \text{ m}$, diameter of wire, $d = 0.5 \text{ mm}$ and resistance of wire, $R = 100 \Omega$

Radius of wire, $r = d/2 = 0.52 \text{ mm}$

$= 0.25 \text{ mm} = 2.5 \times 10^{-4} \text{ m}$

Area of cross-section of wire, $A = \pi r^2$

$\therefore A = 3.14 \times (2.5 \times 10^{-4})^2$

$= 1.9625 \times 10^{-7} \text{ m}^2$

$= 1.9 \times 10^{-7} \text{ m}^2$

As, $R = \rho l/A$

$\therefore 100 \Omega = 1.6 \times 10^{-8} \Omega \text{ m} \times l / 1.9 \times 10^{-7} \text{ m}^2$

$l = 1200 \text{ m}$

If diameter is doubled ($d' = 2d$), then the area of cross-section of wire will become

$A' = \pi r'^2 = \pi (d'/2)^2 = \pi (2d/2)^2 = 4A$

Now $R \propto 1/A$, so the resistance will decrease by four times or new resistance will be

$R' = R/4 = 100/4 = 25 \Omega$

Question 22. The resistance of a wire of 0.01 cm radius is 10 Ω . If the resistivity of the material of the wire is $50 \times 10^{-8} \text{ ohm meter}$, find the length of the wire. (Board Term I, 2014)

Answer: Here, $r = 0.01 \text{ cm} = 10^{-4} \text{ m}$, $\rho = 50 \times 10^{-8} \Omega \text{ m}$ and $R = 10 \Omega$

As, $R = \rho l/A$

or $l = RA/\rho = R \rho (\pi r^2)$

so $l = 10 \times 50 \times 10^{-8} / 3.14 \times (10^{-4})^2$

$= 0.628 \text{ m} = 62.8 \text{ cm}$

Question 23. A wire has a resistance of 16 Ω . It is melted and drawn into a wire of half its original length. Calculate the resistance of the new wire. What is the percentage change in its resistance? (Board Term I, 2013)

Answer: When wire is melted, its volume remains same, so,

$V' = V$ or $A'l' = Al$

Here, $l' = l/2$

Therefore, $A' = 2A$

Resistance, $R = \rho l/A = 16 \Omega$

Now, $R' = \rho l'/A' = \rho (l/2)/2A = 1/4 \rho l/A$

So, $R' = R/4 = 16/4 = 4 \Omega$

Percentage change in resistance,

$$= \frac{(R - R')}{R} \times 100 = \frac{(16 - 4)}{16} \times 100 = 75\%$$

Question 24. If the radius of a current carrying conductor is halved, how does current through it change? (2/5 Board Term I, 2014)

Answer: If the radius of conductor is halved, the area of cross-section reduced to $(1/4)$ of its previous value.

Since, $R \propto 1/A$, resistance will become four times

From Ohm's law, $V = IR$

For given V , $I \propto 1/R$

So, current will reduce to one-fourth of its previous value.

Question 25. Define resistance of a conductor. State the factors on which resistance of a conductor depends. Name the device which is often used to change the resistance without changing the voltage source in an electric circuit. Calculate the resistance of 50 cm length of wire of cross sectional area 0.01 square mm and of resistivity $5 \times 10^{-8} \Omega \text{ m}$. (Board Term I, 2014)

Answer: Resistance is the property of a conductor to resist the flow of charges through it.

Factors affecting resistance of a conductor:

Refer to answer 17(i)

Rheostat is the device which is often used to change the resistance without changing the voltage source in an electric circuit.

We are given, length of wire, $l = 50 \text{ cm} = 50 \times 10^{-2} \text{ m}$ cross-sectional area, $A = 0.01 \text{ mm}^2$
 $= 0.01 \times 10^{-6} \text{ m}^2$

and resistivity, $\rho = 5 \times 10^{-8} \Omega \text{ m}$.

As, resistance, $R = \rho l/A$

$$\therefore R = \frac{5 \times 10^{-8} \times 50 \times 10^{-2}}{0.01 \times 10^{-6}} \Omega$$
$$= 2.5 \Omega$$

Question 26. If a person has five resistors each of value 15Ω , then the maximum resistance he can obtain by connecting them is

- (a) 1Ω
- (b) 5Ω
- (c) 10Ω
- (d) 25Ω (2020)

Answer:

(a) The maximum resistance can be obtained from a group of resistors by connecting them in series. Thus,

$$R_s = 15 + 15 + 15 + 15 + 15 = 75 \Omega$$

Question 27. The maximum resistance which can be made using four resistors each of 2Ω is

- (a) 2Ω
- (b) 4Ω
- (c) 8Ω
- (d) 16Ω (2020)

Answer:

(c) : A group of resistors can produce maximum resistance when they all are connected in series.

$$\therefore R_s = 2 \Omega + 2 \Omega + 2 \Omega + 2 \Omega = 8 \Omega$$

Question 28. The maximum resistance which can be made using four resistors each of resistance 12Ω is

- (a) 2Ω
- (b) 1Ω
- (c) 2.5Ω
- (d) 8Ω (2020)

Answer:

(a) The maximum resistance can be produced from a group of resistors by connecting them in series.

$$\text{Thus, } R_s = 12 \Omega + 12 \Omega + 12 \Omega + 12 \Omega = 48 \Omega$$

Question 29. Three resistors of 10Ω , 15Ω and 5Ω are connected in parallel. Find their equivalent resistance. (Board Term I, 2014)

Answer:

Here, $R_1 = 10 \Omega$, $R_2 = 15 \Omega$, $R_3 = 5 \Omega$.

In parallel combination, equivalent resistance, (R_{eq}) is given by

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\text{So, } \frac{1}{R_{eq}} = \frac{1}{10} + \frac{1}{15} + \frac{1}{5}$$

$$\frac{1}{R_{eq}} = \frac{3+2+6}{30} = \frac{11}{30}$$

$$\therefore R_{eq} = \frac{30}{11} \Omega = 2.73 \Omega$$

Question 30. List the advantages of connecting electrical devices in parallel with an electrical source instead of connecting them in series. (Board Term I, 2013)

Answer:

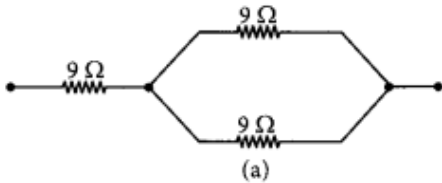
(a) When a number of electrical devices are connected in parallel, each device gets the same potential difference as provided by the battery and it keeps on working even if other devices fail. This is not so in case the devices are connected in series because when one device fails, the circuit is broken and all devices stop working.

(b) Parallel circuit is helpful when each device has different resistance and requires different current for its operation as in this case the current divides itself through different devices. This is not so in series circuit where same current flows through all the devices, irrespective of their resistances.

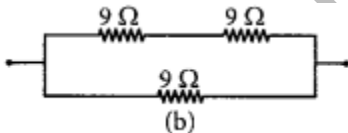
Question 31. Show how would you join three resistors, each of resistance 9Ω so that the equivalent resistance of the combination is (i) 13.5Ω , (ii) 6Ω (2018)

Answer:

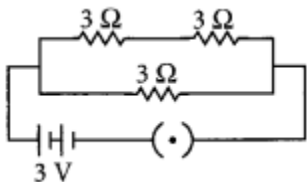
(i) The resistance of the series combination is higher than each of the resistances. A parallel combination of two 9Ω resistors is equivalent to 4.5Ω . We can obtain 13.5Ω by coupling 4.5Ω and 9Ω in series. So, to obtain 13.5Ω , the combination is as shown in figure (a).



(ii) To obtain an equivalent resistance of 6Ω , we have to connect two 9Ω resistors in series and then connect the third 9Ω resistor in parallel to the series combination as shown in the figure (b).



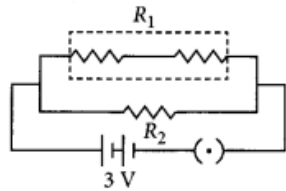
Question 32. Three resistors of 3Ω each are connected to a battery of 3 V as shown. Calculate the current drawn from the battery. (Board Term I, 2017)



Answer: As given in circuit diagram, two 3Ω resistors are connected in series to form R_1 ; so $R_1 = 3 \Omega + 3 \Omega = 6 \Omega$. And, R_1 and R_2 are in parallel combination, Hence, equivalent resistance of circuit (R_{eq}) given by

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\therefore \frac{1}{R_{eq}} = \frac{1}{6} + \frac{1}{3} = \frac{1+2}{6} = \frac{3}{6} = \frac{1}{2}$$



$$R_{eq} = 2 \Omega$$

Using Ohm's law, $V = IR$

We get,

$$3 \text{ V} = I \times 2 \Omega$$

$$\text{or } I = \frac{3 \text{ V}}{2 \Omega} = 1.5 \text{ A}$$

Current drawn from the battery is 1.5 A.

Question 33. Two identical resistors are first connected in series and then in parallel. Find the ratio of equivalent resistance in two cases. (Board Term I, 2013)

Answer: Let resistance of each resistor be R .

For series combination,

$$R_s = R_1 + R_2$$

$$\text{So, } R_s = R + R = 2R$$

For parallel combination,

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} \quad \text{or} \quad R_p = \frac{R_1 R_2}{R_1 + R_2}$$

$$\text{So, } R_p = \frac{R \times R}{R + R} = \frac{R}{2}$$

$$\text{Required ratio} = \frac{R_s}{R_p} = \frac{2R}{R/2} = 4 : 1$$

Question 34. (a) A 6Ω resistance wire is doubled on itself. Calculate the new resistance of the wire.

(b) Three 2Ω resistors A, B and C are connected in such a way that the total resistance of the combination is 3Ω . Show the arrangement of the three resistors and justify your answer. (2020)

Answer:

(a) Given resistance of wire, $R = 6 \Omega$

Let l be the length of the wire and A be its area of cross-section. Then

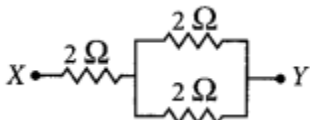
$$R = \rho l A = 6 \Omega$$

Now when the length is doubled, $l' = 2l$ and $A' = A/2$

$$\therefore R' = \rho(2l)A/2 = 4\rho l A = 4 \times 6 \Omega = 24 \Omega$$

(b) Given the total resistance of the combination = 3Ω

In order to get a total resistance of 3Ω , the three resistors has to be connected as shown.



$$\text{Such that, } \frac{1}{R_p} = \frac{1}{2} + \frac{1}{2} = 1$$

$$\Rightarrow R_p = 1 \Omega$$

$$\text{and } R_s = 2 \Omega + 1 \Omega = 3 \Omega$$

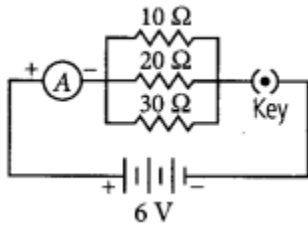
Question 35. Draw a schematic diagram of a circuit consisting of a battery of 3 cells of 2 V each, a combination of three resistors of 10Ω , 20Ω and 30Ω connected in parallel, a plug key and an ammeter, all connected in series. Use this circuit to find the value of the

following :

- (a) Current through each resistor
- (b) Total current in the circuit
- (c) Total effective resistance of the circuit. (2020)

Answer:

The circuit diagram is as shown below.



(a) Given, voltage of the battery = $2V + 2V + 2V = 6V$

Current through 10Ω resistance,

$$I_{10} = \frac{V}{R} = \frac{6}{10} = 0.6A$$

Current through 20Ω resistance,

$$I_{20} = \frac{V}{R} = \frac{6}{20} = 0.3A$$

Current through 30Ω resistance,

$$I_{30} = \frac{V}{R} = \frac{6}{30} = 0.2A$$

(b) Total current in the circuit, $I = I_{10} + I_{20} + I_{30}$

$$= 0.6 + 0.3 + 0.2 = 1.1A$$

(c) Total resistance of the circuit,

$$\frac{1}{R_p} = \frac{1}{10} + \frac{1}{20} + \frac{1}{30} = \frac{6}{60} = \frac{1}{10}$$

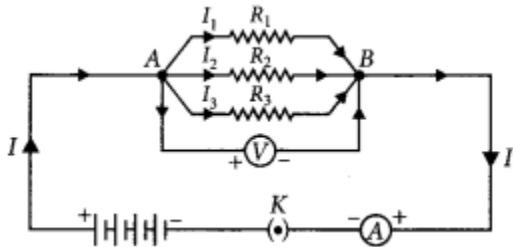
Question 36.

(a) With the help of a suitable circuit diagram prove that the reciprocal of the equivalent resistance of a group of resistances joined in parallel is equal to the sum of the reciprocals of the individual resistances.

(b) In an electric circuit two resistors of 12Ω each are joined in parallel to a $6V$ battery. Find the current drawn from the battery. (Delhi 2019)

Answer:

(a) Resistors in parallel : When resistors are connected in parallel.



(i) The potential difference across their ends is the same.

(ii) The sum of current through them is the current drawn from the source of energy or cell.

$$I = I_1 + I_2 + I_3 \text{ or } \frac{V}{R_p} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

(iii) The equivalent resistance is given by,

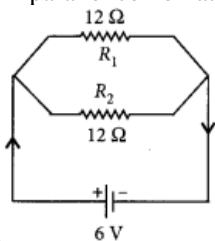
$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

Hence equivalent resistance in parallel combination is equal to the sum of reciprocals of the individual resistances.

$$(b) \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

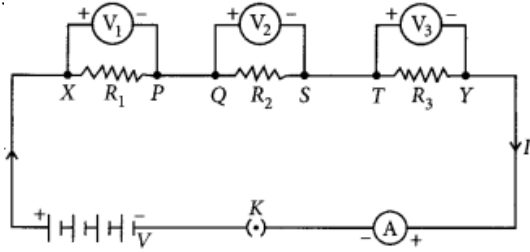
$$\frac{1}{R} = \frac{1}{12} + \frac{1}{12} = \frac{2}{12}$$

$$\Rightarrow R = 6\Omega$$



$$\therefore \text{Current, } I = \frac{V}{R} = \frac{6}{6} = 1A$$

Question 37. For the series combination of three resistors current in each resistor, establish the relation $R = R_1 + R_2 + R_3$ where the symbols have their usual meanings. Calculate the equivalent resistance of the combination of three resistors of 6Ω , 9Ω and 18Ω joined in parallel. (Board Term I. 2016)



Given figure shows the series combination of three resistors R_1 , R_2 and R_3 connected across a voltage source of potential difference V . Let current I is flowing through the circuit.

V_1 , V_2 and V_3 are the potential differences across resistors R_1 , R_2 and R_3 respectively.

Since, the total potential difference across a combination of resistors in series is equal to the sum of potential difference across the individual resistors.

$$\therefore V = V_1 + V_2 + V_3 \dots (i)$$

In series current through each resistor is same. Applying the Ohms law,

$$V_1 = IR_1, V_2 = IR_2 \text{ and } V_3 = IR_3 \dots \dots (ii)$$

If R_s is the equivalent resistance of the circuit, then

$$V = IR_s \dots (iii)$$

From eqns. (i), (ii) and (iii),

$$\text{we can write } IR_s = IR_1 + IR_2 + IR_3$$

$$\text{or } R_s = R_1 + R_2 + R_3$$

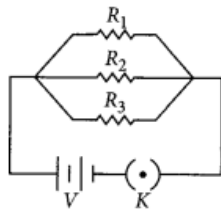
We can conclude that when several resistors are joined in series, the resistance of the combination R_s equals the sum of their individual resistances,

R_1 , R_2 and R_3

Given : $R_1 = 6 \Omega$, $R_2 = 9 \Omega$,

$R_3 = 18 \Omega$ are connected in parallel.

Equivalent resistance, R_{eq} , is given by



$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

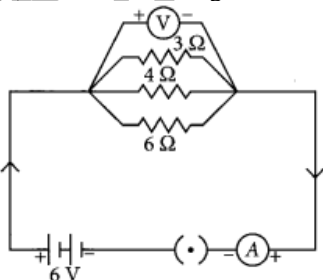
$$\therefore \frac{1}{R_{eq}} = \frac{1}{6} + \frac{1}{9} + \frac{1}{18} = \frac{3+2+1}{18} = \frac{6}{18} = \frac{1}{3}$$

$$\text{or } R_{eq} = 3 \Omega$$

Question 38. State ohms law. Represent it graphically. In the given circuit diagram calculate

(i) the total effective resistance of the circuit.

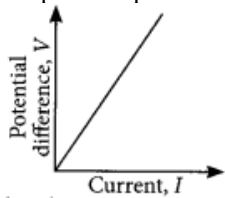
(ii) the current through each resistor.



Answer:

Ohm's law: Refer to answer 7.

Graphical representation of Ohm's law



For the given circuit

$R_1 = 3 \Omega$, $R_2 = 4 \Omega$, $R_3 = 6 \Omega$ and $V = 6V$.

(i) Total effective resistance of the circuit, R_{eq} is given by

$$1R_{eq} = 1R_1 + 1R_2 + 1R_3 = 1/3 + 1/4 + 1/6 = 9/12$$

$$\text{or } R_{eq} = 129 \Omega = 43 \Omega = 1.33 \Omega$$

(ii) Since, potential difference across each resistor connected in parallel is same.

So, $V_1 = V_2 = V_3 = 6V$

Applying Ohm's law,

$$V_1 = I_1 R_1 \text{ or } I_1 = V_1 / R_1 \text{ or } I_1 = 6V / 3\Omega = 2A$$

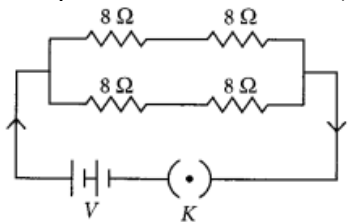
Similarly, $I_2 = 6V / 4\Omega = 1.5A$ and $I_3 = 6V / 6\Omega = 1A$

Question 39. (a) Prove that the equivalent resistance of three resistors R_1 , R_2 and R_3 in series is $R_1 + R_2 + R_3$

(b) You have four resistors of 8Ω each. Show how would you connect these resistors to have effective resistance of 8Ω ? (4/5, Board Term I, 2015)

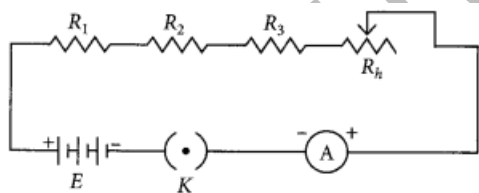
Answer: (a) Refer to answer 37.

(b) If you have four 8Ω resistors and the effective resistance is also 8Ω then the two 8Ω resistors are connected in series. Now you have pair of two 16Ω resistors ($8 \Omega + 8 \Omega$). If you connect these resistors in parallel, you will have net resistance 8Ω .



Question 40. Draw a labelled circuit diagram showing three resistors R_1 , R_2 and R_3 connected in series with a battery (E), a rheostat (R_h), a plug key (K) and an ammeter (A) using standard circuit symbols. Use this circuit to show that the same current flows through every part of the circuit. List two precautions you would observe while performing the experiment. (Board Term I, 2014)

Answer:



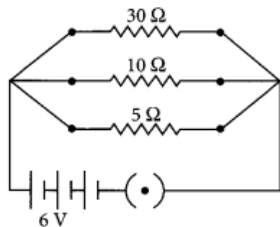
Change the positions of ammeter and note the reading of ammeter each time. You will find that all the reading obtained are same. So, the value of the current in the ammeter is the same, independent of its position in the electric circuit. It means that in this circuit (series combination) the current is the same in every part of the circuit.

Precautions:

(i) All the connections are neat and tight.

(ii) Ammeter is connected with the proper polarity, i.e., positive terminal of the ammeter should go to positive terminal and negative terminal of ammeter to the negative terminal of the battery or cell used.

Question 41. Two wires A and B are of equal length and have equal resistances. If the resistivity of A is more than that of B, which wire is thicker and why? For the electric circuit given below calculate:



- (i) current in each resistor
 (ii) total current drawn from the battery, and
 (iii) equivalent resistance of the circuit. (Board Term I, 2014)

Answer: Let l_A , a_A and R_A be the length, area of cross-section and resistance of wire A and l_B , a_B and R_B are that of wire B. Here, $l_A = l_B$ and $R_A = R_B$

If ρ_A and ρ_B are the resistivities of wire A and B respectively then

$$R_A = \rho_A \frac{l_{AA}}{a_{AA}} \text{ and } R_B = \rho_B \frac{l_{BB}}{a_{BB}}, \text{ As } R_A = R_B$$

$$\therefore \rho_A \frac{l_{AA}}{a_{AA}}, \rho_B \frac{l_{BB}}{a_{BB}}$$

$$\text{or } \rho_{AB} = a_{AB}$$

Since $\rho_A > \rho_B$ therefore $a_A > a_B$ Hence, wire A is thicker than wire B.

For parallel combination,

$$V_1 = V_2 = V_3 = 6V$$

(i) Using Ohm's law

$$I_1 = V_1/R_1 = 6/30 = 0.2 \text{ A}$$

$$I_2 = V_2/R_2 = 6/10 = 0.6 \text{ A}$$

$$I_3 = V_3/R_3 = 6/5 = 1.2 \text{ A}$$

(ii) Total current drawn from battery,

$$I = I_1 + I_2 + I_3 = 0.2 + 0.6 + 1.2 = 2 \text{ A}$$

(iii) Equivalent resistance of the circuit, R_{eq} can be obtained by Ohm's law

$$V = I R_{eq}$$

$$\text{So, } 6 \text{ V} = 2 \text{ A} \times R_{eq} \text{ or, } R_{eq} = 6/2 = 3 \Omega$$

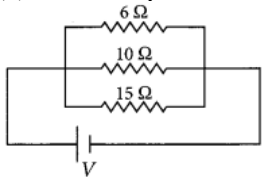
$$\text{Aliter, } \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\frac{1}{R_{eq}} = \frac{1}{30} + \frac{1}{10} + \frac{1}{5} = \frac{1+3+6}{30} = \frac{10}{30} = \frac{1}{3}$$

$$\text{or } R_{eq} = 3 \Omega$$

Question 42. (a) Derive an expression to find the equivalent resistance of three resistors connected in series. Also draw the schematic diagram of the circuit.

(b) Find the equivalent resistance of the following circuit.



Answer: (a) Refer to answer 37.

(b) For the given circuit,

$$R_1 = 6 \Omega, R_2 = 10 \Omega, R_3 = 15 \Omega.$$

$$\text{As } \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\frac{1}{R_{eq}} = \frac{1}{6} + \frac{1}{10} + \frac{1}{15}$$

$$= \frac{5+3+2}{30} = \frac{10}{30} = \frac{1}{3}$$

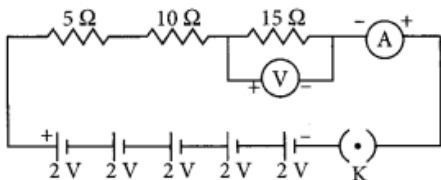
$$R_{eq} = 3 \Omega$$

Question 43. Draw a circuit diagram for a circuit consisting of a battery of five cells of 2 volts each, a 5 Ω resistor, a 10 Ω resistor and a 15 Ω resistor, an ammeter and a plug key, all connected in series. Also connect a voltmeter to record the potential difference across the 15 Ω resistor and calculate

(i) the electric current passing through the above circuit and

(ii) potential difference across 5 Ω resistor when the key is closed. (Board Term 1, 2013)

Answer:



Potential of the battery, $V = (2 \times 5) \text{ V} = 10 \text{ V}$

Equivalent resistance,

$$R_{\text{eq}} = R_1 + R_2 + R_3$$

$$= (5 + 10 + 15)\Omega = 30 \Omega$$

(i) Current through circuit, $I = \frac{VR}{1030} \text{ A} = 13 \text{ A}$

(ii) Potential across 5Ω resistor, $V_1 = IR_1$

$$= 13 \times 5 = 53 \text{ V} = 1.67 \text{ V}$$

Question 44. The resistance of a resistor is reduced to half of its initial value. In doing so, if other parameters of the circuit remain unchanged, the heating effects in the resistor will become

- (a) two times
- (b) half
- (c) one-fourth
- (d) four times (2020)

Answer:

(a) : We know, $H = I^2 R t = \frac{V^2}{R} t$

Now when, $R' = \frac{R}{2}$, $V' = V$ and $t' = t$

$$H' = \frac{V^2 t'}{R'} = \frac{V^2 t R}{2} = 2V^2 t R = 2H$$

Question 45.

- (a) Write the mathematical expression for Joules law of heating.
- (b) Compute the heat generated while transferring 96000 coulomb of charge in two hours through a potential difference of 40 V. (2020)

Answer:

(a) The Joule's law of heating implies that heat produced in a resistor is

- (i) directly proportional to the square of current for a given resistance,
- (ii) directly proportional to resistance for a given current, and
- (iii) directly proportional to the time for which the current flows through the resistor.

$$\text{i.e., } H = I^2 R t$$

(b) Given, charge $q = 96000 \text{ C}$, time $t = 2 \text{ h} = 7200 \text{ s}$ and potential difference $V = 40 \text{ V}$

$$\text{We know, } H = I^2 R t = \frac{Q^2}{t} \times \frac{V}{Q} \times t = VQ$$

$$= 40 \times 96000 = 3.84 \times 10^6 \text{ J} = 3.84 \text{ MJ}$$

Question 46. Write Joules law of heating. (1/3, 2018)

Answer: Refer to answer 45(a).

Question 47. Explain the use of an electric fuse. What type of material is used for fuse wire and why? (Board Term I, 2016)

Answer: Electric fuse protects circuits and appliances by stopping the flow of any unduly high electric current. It consists of a piece of wire made of a metal or an alloy of appropriate melting point, for example aluminium, copper, iron, lead etc. If a current larger than the specified value flows through the circuit, the temperature of the fuse wire increases. This melts the fuse wire and breaks the circuit.

Question 48. (a) Why is tungsten used for making bulb filaments of incandescent lamps?

(b) Name any two electric devices based on heating effect of electric current. (2/5, Board Term I, 2015)

Answer:

- (a) (i) Tungsten is a strong metal and has high melting point (3380°C).
- (ii) It emits light at high temperatures (about 2500°C).
- (b) Electric laundry iron and electric heater are based on heating effect of electric current.

Question 49. A fuse wire melts at 5 A. If it is desired that the fuse wire of same material melt at 10 A, then whether the new fuse wire should be of smaller or larger radius than the earlier one? Give reasons for your answer. (3/5, Board Term I, 2014)

Answer: Let the resistance of the wire be R , heat produced in the fuse at 5 A in I_s is

$$H = I^2 R t$$

50. fuse melts at $(5)^2 R$ joules of heat.

Let, the resistance of new wire is R'

So, heat produced in 1 second = $(10)^2 R'$

To prevent it from melting

$$(5)^2 R = (10)^2 R' \text{ or } R' = R/4$$

As $R \propto 1/A$

\therefore cross-sectional area of new fuse wire is four times the first fuse.

Now, $A = \pi r^2$, so new radius is twice the previous one. So, at 10 A, the new fuse wire of same material and length has larger radius than the earlier one.

Question 50. What is heating effect of current? List two electrical appliances which work on this effect. (2/5, Board Term I, 2013)

Answer: If only resistors are connected to the battery, the source energy continually gets dissipated entirely in the form of heat. This is known as heating effect of current, 'file amount of heat (H) produced in time t is given by Joule's law of heating.

$$H = I^2 R t$$

Where, I is current flowing through resistor R .

The electric laundry iron, electric toaster, electric oven, electric kettle and electric heater are some common devices based on heating effect of current.

Question 51. Two bulbs of 100 W and 40 W are connected in series. The current through the 100 W bulb is 1 A. The current through the 40 W bulb will be

- (a) 0.4 A
- (b) 0.6 A
- (c) 0.8 A
- (d) 1 A (2020)

Answer: (d) : Given power of first bulb, $P_1 = 100$ W and second bulb $P_2 = 40$ W

Current through 100 W bulb, $I_1 = 1$ A

Current through 40 W bulb, $I_2 = ?$

Since both the bulbs are connected in series, the electric current passing through both the bulbs are same i.e., $I_2 = 1$ A.

Question 52. Write the relation between resistance (R) of filament of a bulb, its power (P) and a constant voltage V applied across it. (Board Term I, 2017)

$$\text{Answer: } P = V^2/R$$

Question 53. Power of a lamp is 60 W. Find the energy in joules consumed by it in 1 s. (Board Term I, 2016)

Answer: Here, power of lamp, $P = 60$ W time,

$t = 1$ s

So, energy consumed = Power \times time = $(60 \times 1) \text{ J} = 60$ J

Question 54. Two lamps, one rated 100 W; 220 V, and the other 60 W; 220 V, are connected in parallel to electric mains supply. Find the current drawn by two bulbs from the line, if the supply voltage is 220 V. (2/3, 2018, Board Term I, 2014)

Answer: Since both the bulbs are connected in parallel and to a 220 V supply, the voltage across each bulb is 220 V. Then

Current drawn by 100 W bulb,

$$I_1 = \frac{\text{power}}{\text{rating voltage applied}} = \frac{100 \text{ W}}{220 \text{ V}} = 0.454 \text{ A}$$

Current drawn by 60 W bulb,

$$I_2 = \frac{60 \text{ W}}{220 \text{ V}} = 0.273 \text{ A}$$

Total current drawn from the supply line,

$$I = I_1 + I_2 = 0.454 \text{ A} + 0.273 \text{ A} = 0.727 \text{ A} = 0.73 \text{ A}$$

Question 55. How much current will an electric iron draw from a 220 V source if the resistance of its element when hot is 55 ohms? Calculate the wattage of the electric iron when it operates on 220 volts. (Board Term I, 2016)

Answer: Here, $V = 220$ V, $R = 55 \Omega$

By Ohm's law $V = IR$

$$\therefore 220 = I \times 55 \text{ or } I = 4 \text{ A}$$

Wattage of electric iron = Power

$$= V I = (220) \times 4 = 880 \text{ W}$$

Question 56. An electric iron has a rating of 750 W; 200 V. Calculate:

- (i) the current required.
- (ii) the resistance of its heating element.
- (iii) energy consumed by the iron in 2 hours. [Board Term 1, 2015]

Answer: Here, $P = 750 \text{ W}$, $V = 200 \text{ V}$

(i) As $P = VI$

$$I = P/V = (750/200) \text{ A} = 3.75 \text{ A}$$

(ii) By Ohm's law $V = IR$ or $R = V/I$

$$\therefore R = 200/3.75 \Omega = 53.3 \Omega$$

(iii) Energy consumed by the iron in 2 hours

$$= P \times t = 750 \text{ W} \times 2 \text{ h} = 1.5 \text{ kWh}$$

$$\text{or } E = (750 \times 2 \times 3600) \text{ J} = 5.4 \times 10^6 \text{ J}$$

Question 57. An electric bulb is connected to a 220 V generator. The current is 2.5 A. Calculate the power of the bulb. (1/3, Board Term I, 2015)

Answer: Here, $V = 220 \text{ V}$, $I = 2.5 \text{ A}$

$$\text{Power of the bulb } P = VI = 220 \times 2.5 \text{ W} = 550 \text{ W}$$

Question 58. (a) Define power and state its SI unit.

(b) A torch bulb is rated 5 V and 500 mA. Calculate its

- (i) power
- (ii) resistance
- (iii) energy consumed when it is lighted for 2 1/2 hours.

Answer: (a) Power is defined as the rate at which electric energy is dissipated or consumed in an electric circuit.

$$P = VI = I^2R = V^2/R$$

The SI unit of electric power is watt (W). It is the power consumed by a device that carries 1 A of current when operated at a potential difference of 1 V.

$$1 \text{ W} = 1 \text{ volt} \times 1 \text{ ampere} = 1 \text{ V A}$$

(b) Given, $V = 5 \text{ V}$ and $I = 500 \text{ mA} = 0.5 \text{ A}$

$$(i) \text{ Power, } P = V \times I = 5 \times 0.5 = 2.5 \text{ W}$$

$$(ii) \text{ As, } P = V^2/R \Rightarrow R = V^2/P = 25/2.5 = 10 \Omega$$

(iii) Given, time $t = 2.5 \text{ hrs} = 9000 \text{ s}$

$$\therefore \text{The energy consumed, } E = P \times t$$

$$= 2.5 \times 9000 = 2.25 \times 10^4 \text{ J}$$

$$= 6.25 \text{ Watt hour}$$

Question 59. Two identical resistors, each of resistance 15Ω , are connected in (i) series, and (ii) parallel, in turn to a battery of 6 V. Calculate the ratio of the power consumed in the combination of resistors in each case. (2020)

Answer: Given, $R_1 = R_2 = 15 \Omega$, $V = 6 \text{ V}$

(i) When connected in series,

$$R_s = R_1 + R_2 = 15 \Omega + 15 \Omega = 30 \Omega$$

$$\text{Power, } P_s = V^2/R_s = 36/30 \text{ W}$$

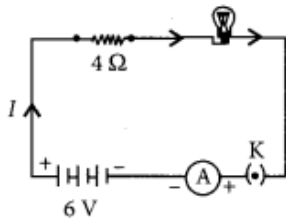
(ii) When connected in parallel,

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} \Rightarrow R_p = \frac{15}{2} \Omega$$

$$\therefore \text{Power, } P_p = \frac{V^2}{R_p} = \frac{36}{15} \times 2 \text{ W}$$

$$\therefore \text{The ratio, } \frac{P_s}{P_p} = \frac{36}{30} \times \frac{15}{36 \times 2} = \frac{1}{4}$$

Question 60. An electric lamp of resistance 20Ω and a conductor of resistance 4Ω are connected to a 6 V battery as shown in the circuit. Calculate.



- (a) the total resistance of the circuit
 (b) the current through the circuit,
 (c) the potential difference across the (i) electric lamp and (ii) conductor, and
 (d) power of the lamp. (Delhi 2019)

Answer: Resistance of the lamp = $20\ \Omega$

External resistance = $4\ \Omega$

(a) As both the lamp and external resistance are connected in series, therefore the total resistance,
 $R = 20 + 4 = 24\ \Omega$

(b) Current, $I = \frac{VR}{624} = 0.25\ \text{A}$

(c) (i) Potential difference across the electric lamp

$\text{Total voltage} \times \frac{\text{resistance of lamp}}{\text{Total resistance}}$
 $= 624 \times \frac{20}{24} = 5\ \text{V}$

(ii) Potential difference across conductor

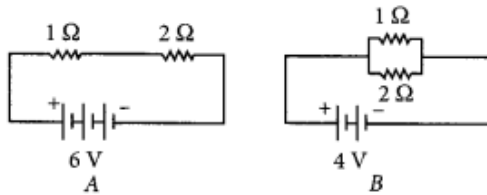
$\text{Total voltage} \times \frac{\text{resistance of conductor}}{\text{Total resistance}}$
 $= 624 \times \frac{4}{24} = 1\ \text{V}$

(d) Power of the lamp

$= (\text{current})^2 \times \text{resistance of lamp}$

$= (0.25)^2 \times 20 = 1.25\ \text{W}$

Question 61. Compare the power used in $2\ \Omega$ resistor in each of the following circuits. (AI 2019)



Answer: In circuit A,

Total resistance, $R = 1 + 2 = 3\ \Omega$

Voltage across $2\ \Omega = \frac{V_{\text{Total}} R_{\text{Total}}}{R_{\text{Total}}} \times 2\ \Omega = \frac{6 \times 2}{3} = 4\ \text{V}$

\therefore Power used in $2\ \Omega$ resistor,

$p = \frac{V^2}{R} = \frac{(4)^2}{2} = 8\ \text{w}$

In circuit B, Voltage across both the resistance is same i.e. $4\ \text{V}$ and both are connected in parallel combination.

\therefore Power used in $2\ \Omega$ resistor = $\frac{V^2}{R} = \frac{(4)^2}{2} = 8\ \text{w}$

\therefore Power used in $2\ \Omega$ resistor in each case is same i.e. $8\ \text{W}$.

Question 62. A bulb is rated $40\ \text{W}; 220\ \text{V}$. Find the current drawn by it, when it is connected to a $220\ \text{V}$ supply. Also find its resistance. If the given bulb is replaced by a bulb of rating $25\ \text{W}; 220\ \text{V}$, will there be any change in the value of current and resistance? Justify your answer and determine the change. (AI 2019)

Answer: In first case, $P = 40\ \text{W}$, $V = 220\ \text{V}$

Current drawn $I = \frac{PV}{40 \times 220} = 0.18\ \text{A}$

Also, resistance of bulb,

$R = \frac{V^2}{P} = \frac{(220)^2}{40} = 1210\ \Omega$

In second case, $P = 25\ \text{W}$, $V = 220\ \text{V}$

Current drawn, $I = \frac{PV}{25 \times 220} = 0.11\ \text{A}$

Also, resistance of the bulb,

$R = \frac{V^2}{P} = \frac{(220)^2}{25} = 1936\ \Omega$

Hence, by replacing $40\ \text{W}$ bulb to $25\ \text{W}$ bulb, having same source of voltage the amount of current flows decreases while resistance increases.

Question 63. (a) How two resistors, with resistances $R_1 \Omega$ and $R_1 \Omega$ respectively are to be connected to a battery of emf V volts so that the electrical power consumed is minimum?

(b) In a house 3 bulbs of 100 watt each lighted for 5 hours daily, 2 fans of 50 watt each used for 10 hours daily and an electric heater of 1.00 kW is used for half an hour daily. Calculate the total energy consumed in a month of 31 days and its cost at the rate of Rs 3.60 per kWh. (Board Term I, 2017)

Answer: (a) Power consumed is minimum when current through the circuit is minimum, so the two resistors are connected in series.

(b) Power of each bulb $P_1 = 100$ watt

Total power of 3 bulbs, $P_1 = 3 \times 100 = 300$ watt

Energy consumed by bulbs in 1 day

$$E_1 = P_1 \times t = 300 \text{ watt} \times 5 \text{ hours.}$$

$$= 1500 \text{ Wh} = 1.5 \text{ kWh}$$

Power of each fan = 50 watt

Total power of 2 fans = 2×50 watt

$$P_2 = 100 \text{ watt}$$

Energy consumed by fans in 1 day

$$E_2 = P_2 \times t = 100 \text{ watt} \times 10 \text{ hours}$$

$$= 1000 \text{ watt hour} = 1 \text{ kWh}$$

Energy consumed by heater,

$$E_3 = 1 \text{ kW} \times 1/2 \text{ h} = 0.5 \text{ kWh}$$

Total energy consumed in one day

$$E = E_1 + E_2 + E_3 = (1.5 + 1 + 0.5) \text{ kWh} = 3 \text{ kWh}$$

Total energy consumed in a month of 31 days

$$= E \times 31 = (3 \times 31) \text{ kWh} = 93 \text{ kWh}$$

$$\text{Cost of energy consumed} = \text{Rs } (93 \times 3.60) = \text{Rs } 334.80$$

Question 64. (a) An electric bulb is connected to a 220 V generator. If the current drawn by the bulb is 0.50 A, find its power.

(b) An electric refrigerator rated 400 W operates 8 hours a day. Calculate the energy per day in kWh.

(c) State the difference between kilowatt and kilowatt hour. (3/5, Board Term I, 2013)

Answer: (a) Here, $V = 220 \text{ V}$, $I = 0.50 \text{ A}$

$$\text{Power of the bulb, } P = VI = (220 \times 0.5) \text{ W} = 110 \text{ W}$$

(b) Energy consumed by electric refrigerator in a day = Power \times time

$$= 400 \text{ W} \times 8 \text{ h} = 3200 \text{ Wh} = 3.2 \text{ kWh}$$

(c) Kilowatt is unit of power and kilowatt hour is a unit of energy.

Question 65. (i) State one difference between kilowatt and kilowatt hour. Express 1 kWh in joules.

(ii) A bulb is rated 5V; 500 mA. Calculate the rated power and resistance of the bulb when it glows. (Board Term I, 2013)

Answer: (i) Refer to answer 64(c).

$$1 \text{ kWh} = 1000 \text{ W} \times 1 \text{ h}$$

$$= 1000 \text{ W} \times 3600 \text{ s} = 3600000 \text{ J} = 3.6 \times 10^6 \text{ J}$$

(ii) Here, $V = 5 \text{ V}$, $I = 500 \text{ mA} = 0.5 \text{ A}$

Power rating of bulb is

$$P = VI = (5 \times 0.5) \text{ W} = 2.5 \text{ W}$$

$$\text{Resistance of the bulb is } R = V/I = (5/0.5) \Omega = 10 \Omega$$